The Quantum Interactive Learning Tutorials (QuILTs) are research-based learning tools based on the investigation of students' common difficulties in learning quantum mechanics. The QuILTs are suitable for upper-level undergraduate quantum mechanics courses. They can either be used as an in-class tutorial on which two or three students can work together with full class discussion and instructor feedback as appropriate, or they can be given as homework supplements.

The pre-test should be administered in class after traditional instruction but before using a QuILT. The tutorial can be distributed to students in the same class after the pre-test. In some QuILTs, there are also warm-ups (that students must work on at home before working on a tutorial) and homework sections (after working on the tutorial) as supplements to the tutorials. Since all students cannot finish the tutorial in one class-period, it is better to administer the post-test in the next class so that all students have adequate opportunity to finish it.

The tutorial development goes through a cyclical iterative process that includes research on student difficulties in learning a particular physics concept, followed by the development, evaluation and refinement of the material. The following features of the QuILTs make them particularly suited for the challenging task of teaching quantum physics:

- 1. They are based upon research in physics education and pay particular attention to cognitive issues.
- 2. They employ visualization tools to help students build physical intuition about quantum processes.
- 3. They consistently keep students actively engaged in the learning process by asking them to predict what should happen in a particular situation and then providing appropriate feedback.
- 4. They attempt to bridge the gap between the abstract quantitative formalism of quantum mechanics and the qualitative understanding necessary to explain and predict diverse physical phenomena without dumbing down the content.
- 5. They are based on systematic investigations of difficulties students have in learning various concepts in quantum physics.
- 6. They can be used in class by the instructors once or twice a week as supplements to lectures or outside of the class as homework or as self-study tool by students.
- 7. They consist of self-sufficient modular units that can be used in any order that is convenient.

A majority of the computer-based visualization tools for this project are being developed by M. Belloni and W. Christian at Davidson College under the Open Source Physics (OSP) project (see http://www.opensourcephysics.org/projects/packages/index.html)

However, some computer-based visualization tools are adapted from Phet simulations (see http://phet.colorado.edu)

## Related References below are at https://sites.google.com/site/professorsinghswebpage/

"Student difficulties with with quantum states while translating state vectors in Dirac notation to wave functions in position and momentum representations", E. Marshman and C. Singh, Proceedings of the 2015 Phys. Ed. Res. Conference, College Park, MD, (D. Jones, A. Churukian, L. Ding Eds.), (2015).

"Investigating transfer of learning in advanced quantum mechanics", A. Maries, R. Sayer and C. Singh, Proceedings of the 2015 Phys. Ed. Res. Conference, College Park, MD, (D. Jones, A. Churukian, L. Ding Eds.), (2015).

"Developing a quantum interactive learning tutorial on the double-slit experiment", R. Sayer, A. Maries and C. Singh, Proceedings of the 2015 Phys. Ed. Res. Conference, College Park, MD, (D. Jones, A. Churukian, L. Ding Eds.), (2015).

"The effect of giving explicit incentives to correct mistakes on subsequent problem solving in quantum mechanics", B. Brown, A. J. Mason and C. Singh, Proceedings of the 2015 Phys. Ed. Res. Conference, College Park, MD, (D. Jones, A. Churukian, L. Ding Eds.), (2015).

"Developing an interactive tutorial on a quantum eraser", E. Marshman and C. Singh, Proceedings of the 2014 Phys. Ed. Res. Conference, Minneapolis, MN, (P. Engelhardt, A. Churukian, D. Jones Eds.) (2015).

"Developing an interactive tutorial on a Mach-Zehnder interferometer with single photons", C. Singh and E. Marshman, Proceedings of the 2014 Phys. Ed. Res. Conference, Minneapolis, MN, (P. Engelhardt, A. Churukian, D. Jones Eds.) (2015).

"Development and evaluation of a quantum interactive learning tutorial on Larmor Precession of spin", B. Brown and C. Singh, Proceedings of the 2014 Phys. Ed. Res. Conference, Minneapolis, MN (A. Churukian, P. Engelhardt, D. Jones Eds.), (2015).

"Development of an interactive tutorial on quantum key distribution", S. DeVore and C. Singh, Proceedings of the 2014 Phys. Ed. Res. Conference, Minneapolis, MN (A. Churukian, P. Engelhardt, D. Jones Eds.), (2015).

Framework for understanding the patterns of student difficulties in quantum mechanics, E. Marshman and C. Singh, PRST-PER 11, 020119 (1-26) (2015).

Review of student difficulties in upper-level quantum mechanics, C. Singh and E. Marshman, PRST-PER 11, 020117 (1-24) (2015).

"Analogous patterns of student reasoning difficulties in introductory physics and upper-level quantum mechanics", C. Singh and E. Marshman, Proceedings of the 2013 Phys. Ed. Res. Conference, Portland, OR, (A. Churukian, P. Engelhardt, D. Jones Eds.), 46-49 (2014).

"Investigating student difficulties with time-dependence of expectation values in quantum mechanics", E. Marshman and C. Singh, Proceedings of the 2013 Phys. Ed. Res. Conference, Portland, OR, (A. Churukian, P. Engelhardt, D. Jones Eds.), 245-248, (2014).

" Investigating student difficulties with Dirac Notation ", C. Singh and E. Marshman, Proceedings of the 2013 Phys. Ed. Res. Conference, Portland, OR, (A. Churukian, P. Engelhardt, D. Jones Eds.), 345-348,(2014). "Improving Student Understanding of Addition of Angular Momentum in Quantum Mechanics ", G. Zhu and C. Singh, Phys. Rev. ST PER, 9(1), 010101 (1-12) (2013).

Improving Students' Understanding of Quantum Mechanics, G. Zhu, Ph.D. Dissertation, University of Pittsburgh, 2011.

"Surveying students' understanding of quantum mechanics in one spatial dimension", G. Zhu and C. Singh, *Am. J. Phys.*, **80**(3), 252-259 (2012).

"Improving students' understanding of quantum measurement I: Investigation of difficulties", G. Zhu and C. Singh, *Phys. Rev. ST PER*, **8**(1), 010117 (1-8) (2012).

"Improving students' understanding of quantum measurement II: Development of Researchbased learning tools", G. Zhu and C. Singh, *Phys. Rev. ST PER*, **8**(1), 010118 (1-13) (2012).

"Improving Students' Understanding of Quantum Mechanics By Using Peer Instruction Tools", C. Singh and G. Zhu, Proceedings of the Phys. Ed. Res. Conference, Omaha, NE, (S. Rebello, C. Singh, P. Engelhardt Eds.), AIP Conf. Proc., Mellville, New York **1413**, 77-80 (2012).

"Students' understanding of the addition of angular momentum", C. Singh and G. Zhu, Proceedings of the Phys. Ed. Res. Conference, Omaha, NE, (S. Rebello, C. Singh, P. Engelhardt Eds.), *AIP Conf. Proc.*, Melville, New York **1413**, 355-358 (2012).

"Students' difficulties with quantum measurement", G. Zhu and C. Singh, Proceedings of the Phys. Ed. Res. Conference, Omaha, NE, (S. Rebello, C. Singh, P. Engelhardt Eds.), *AIP Conf. Proc.*, Melville, New York **1413**, 387-390 (2012).

"Improving students' understanding of quantum mechanics via Stern-Gerlach experiment", G. Zhu and C. Singh, *American Journal of Physics*, **79** (5), 499-507, (2011).

Improving students' understanding of quantum measurement ", G. Zhu and C. Singh, Proceedings of the Phys. Ed. Res. Conference, Portland, OR, (C. Singh, M. Sabella, S. Rebello Eds.), *AIP Conf. Proc.*, Melville, New York **1289**, 345-348 (2010).

"Surveying students' understanding of quantum mechanics", G. Zhu and C. Singh, Proceedings of the Phys. Ed. Res. Conference, Portland, OR, (C. Singh, M. Sabella, S. Rebello Eds.), *AIP Conf. Proc.*, Melville, New York **1289**, 301-304 (2010).

"Surveying Instructors' Attitudes and Approaches to Teaching Quantum Mechanics", S. Siddiqui and C. Singh, Proceedings of the Phys. Ed. Res. Conference, Portland, OR, (C. Singh, M. Sabella, S. Rebello Eds.), AIP Conf. Proc., Melville, New York **1289**, 297-300 (2010).

"Do advanced students learn from their mistakes without explicit intervention?", A. J. Mason and C. Singh, *Am. J. Phys.*, **78**(7), 760-767, (2010).

"Categorization of quantum mechanics problems by professors and students", S. Y. Lin and C. Singh, *Euro. J. Phys.* **31**, 57-68 (2010).

"Students' Understanding of the Stern-Gerlach Experiment", G. Zhu and C. Singh, Proceedings of the Phys. Ed. Res. Conference, Ann Arbor, MI, (C. Henderson, M. Sabella, C. Singh Eds.), *AIP Conf. Proc.*, Melville, New York **1179**, 309-312 (2009).

"Peer Instruction for Quantum Mechanics", G. Zhu and C. Singh, APS Forum on Education Newsletter, 8-10, Fall (2009).

"Reflection and Self-monitoring in Quantum Mechanics", A. Mason and C. Singh, Proceedings of the Phys. Ed. Res. Conference, Ann Arbor, MI, (C. Henderson, M. Sabella, C. Singh Eds.), *AIP Conf. Proc.*, Melville, New York **1179**, 197-200 (2009).

"Assessing Expertise in Quantum Mechanics using Categorization Task", S. Y. Lin and C. Singh, Proceedings of the Phys. Ed. Res. Conference, Ann Arbor, MI, (C. Henderson, M. Sabella, C. Singh Eds.), *AIP Conf. Proc.*, Melville, New York **1179**, 185-188 (2009).

"Cognitive Issues in Learning Advanced Physics: An Example from Quantum Mechanics", C. Singh and G. Zhu, Proceedings of the Phys. Ed. Res. Conference, Ann Arbor, MI, (C. Henderson, M. Sabella, C. Singh Eds.), *AIP Conf. Proc.*, Melville, New York **1179**, 63-66 (2009).

"Interactive Learning Tutorials on Quantum Mechanics", C. Singh, *Am. J. Phys.*, **76**(4), 400-405, (2008).

"Student Understanding of Quantum Mechanics at the Beginning of Graduate Instruction", C. Singh, *Am. J. Phys.*, **76**(3), 277-287, (2008).

"Student Difficulties with Quantum Mechanics Formalism", C. Singh, Proceedings of the Phys. Ed. Res. Conference, Syracuse, NY, (L. McCullough, P. Heron, L. Hsu Eds.), *AIP Conf. Proc.*, Melville New York **883**, 185-188, (2007).

"Helping Students Learn Quantum Mechanics for Quantum Computing", C. Singh, Proceedings of the Phys. Ed. Res. Conference, Syracuse, NY, AIP, (L. McCullough, P. Heron, L. Hsu Eds.), *AIP Conf. Proc.*, Melville New York **883**, 42-45, (2007).

"Improving Student's Understanding of Quantum Mechanics", Feature Article, *Physics Today*, C. Singh, M. Belloni, W. Christian, **8**, 43-49, August (2006). This article was especially selected and translated into Japanese for publication in the first (special) edition of the Japanese version of Physics Today titled Parity, (2007).

"Assessing and Improving Student Understanding of Quantum Mechanics", C. Singh, Proceedings of the Phys. Ed. Res. Conference, Salt Lake City, (P. Heron, J. Marx, L. McCullough Eds.), *AIP Conf. Proc.*, Melville New York **818**, 69-72, (2006).

"Transfer of Learning in Quantum Mechanics", C. Singh, Proceedings of the Phys. Ed. Res. Conference, Sacramento, CA (Eds. P. Heron, S. Franklin, and J. Marx), *AIP Conf. Proc.*, Melville New York **790**, 23-26, (2005).

"Student Understanding of Quantum Mechanics", C. Singh, Am. J. Phys., 69 (8), 885-895, (2001).